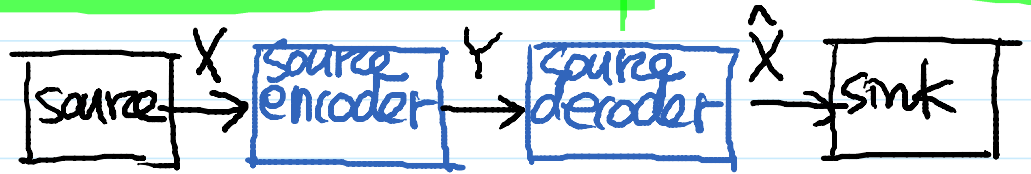


Review



Preview

Data compression
Data transmission

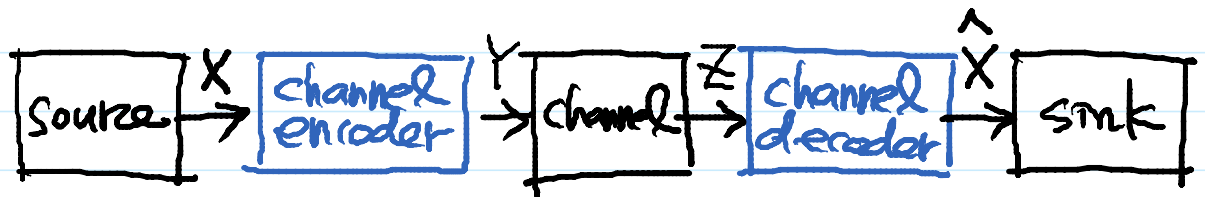


performance evaluation

"Two performance metrics"

(f) meter

< compression error > rates

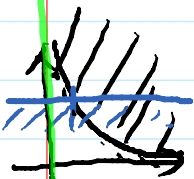


* R. Gallager

I.T.R.C.

"Two performance metrics"

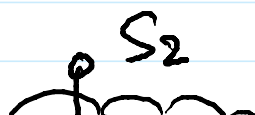
< transmission error > rates



single-source single-destination < DC DT

multiple-source multiple-destination < DC DT

→ Network Information Theory





Probability, Random Variables and Processes
Optimization
Estimation & Detection Theory

Data Compression

☹️?

😊!

Simplify!

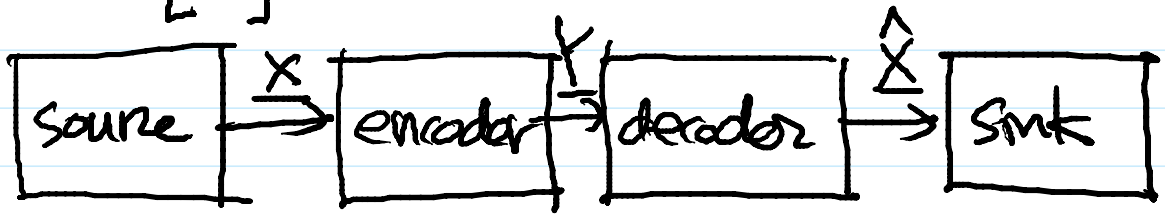
Zero-error data compression

Non-zero error

error-rate is zero!

abstract to concrete.

$$\underline{X} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ \vdots \end{bmatrix} \in \{0, 1\}^{100} \quad \text{of } \mathbb{R}^3$$



$$\underline{X} \in \left\{ \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \end{bmatrix} \right\},$$

$$X \sim \begin{aligned} \Pr(X=0) &= \frac{1}{4} \\ \Pr(X=1) &= \frac{1}{4} \\ \Pr(X=2) &= \frac{1}{2} \end{aligned}$$

$\log_2 3$ bits

x	y
0	00
1	01
2	1

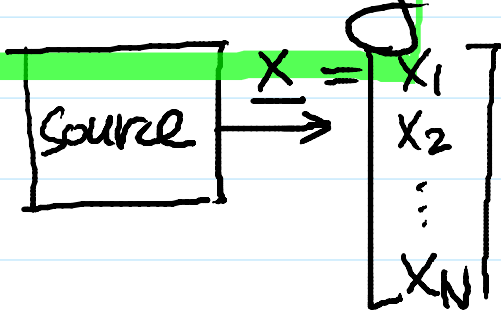
$$\begin{aligned} 2 \times \frac{1}{4} \\ 2 \times \frac{1}{4} \\ \hline 1 \times \frac{1}{2} \end{aligned}$$

1.5 bits

$$= \frac{\log_{10} 3}{\log_{10} 2}$$

$$\approx \frac{0.4771}{0.3010} \approx 1.585 \text{ bits}$$

Source modeling



- X_i 's are i.i.d.
- X_i 's are discrete.
- (X : sample space)
- X is finite.

Simplify!

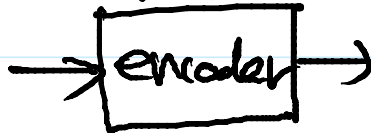
Independent and identically distributed (i.i.d.)

Google advanced search

"....." site:.edu

encoder modeling

↳ a mapping rule



$$\underline{Y} = \begin{bmatrix} Y_1 \\ \vdots \\ Y_N \end{bmatrix}$$

(domain, mapping rule, range)

$$(X^N, \quad \quad \quad)$$

~~$\mathcal{Q}^*$~~

$$Y_i \in \mathcal{Q}$$

$$\mathcal{Q}^*$$

Variable-length source coding

binary
ternary
quaternary
i

Example

$$\mathcal{Q} = \{0, 1\}$$

$$\mathcal{Q}^* = \{[0], [1],$$

$$[00], [01], \dots$$

$$\dots \quad \quad \quad \}$$

$$\mathcal{Q}^*$$

$$|\mathcal{Q}^*| = \infty$$

$$|\mathcal{Q}^*| = N$$

D-ary encoder $|Q| = D$

D # of D-ary symbols

$$2^{100} = 4^{50} = (2^2)^{50} = 2^{100}$$

< source alphabet: X
code alphabet: Q

the Law of Large Numbers. $\swarrow$ s.l.l.n
w.l.l.n
 $\rightarrow$ Expectation! 😊