

Review

single-source single-destination

< data compression
data transmission

Two performance metrics

< compression rate vs. error rate
transmission rate vs. error rate

Zero-error data compression

minimize $L(\mathcal{C})$

$\mathcal{C}$

subject to $\mathcal{C}$ is UD.

x	$P(X=x)$
1	p_1
2	p_2
$\vdots$	$\vdots$
$ x $	$p_{ x }$

x	$C(x)$	$l(x)$
1	c_1	l_1
2	c_2	l_2
$\vdots$	$\vdots$	$\vdots$
$ x $	$c_{ x }$	$l_{ x }$

variable-length source code

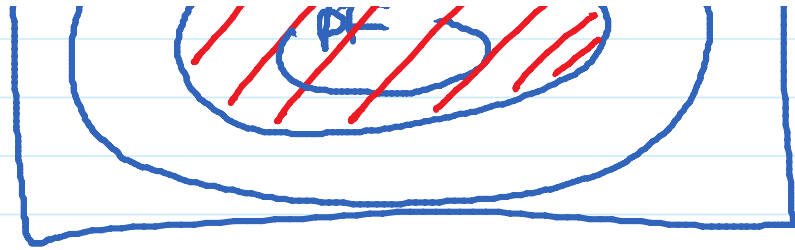
mathematical calligraphize. $L(\mathcal{C}) = E\{l(x)\}$

all v.l. s.c. $= \sum_{i=1}^{|x|} p_i l_i$

non-singular

UD

PF



$$\text{lower bound} \leq \min_{e \in \text{BUD}} L(e) \leq \text{upper bound}$$

ef) bounds $\begin{cases} \text{upper} \\ \text{lower} \end{cases}$

bounds $\begin{cases} \text{loose} \\ \text{tight} \end{cases}$

$$H_0(X) \leq \min_{e \in \text{BUD}} L(e) < H_0(X) + 1$$

• Entropy lower Bound

- If $\mathcal{C}$ is $\uparrow$ UD, then $\sum_{i=1}^{|\mathcal{C}|} D^{-l_i} \leq 1$
 a Dary

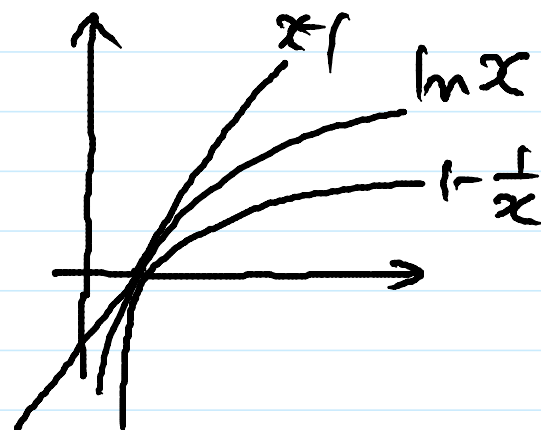
Kraft's inequality

- If $\mathcal{C}$ is UD, then $H_D(X) \leq L(\mathcal{C})$

- $1 - \frac{1}{x} \leq \ln x \leq x - 1$

$\sim$
iff $x=1$

$\sim$
iff $x=1$

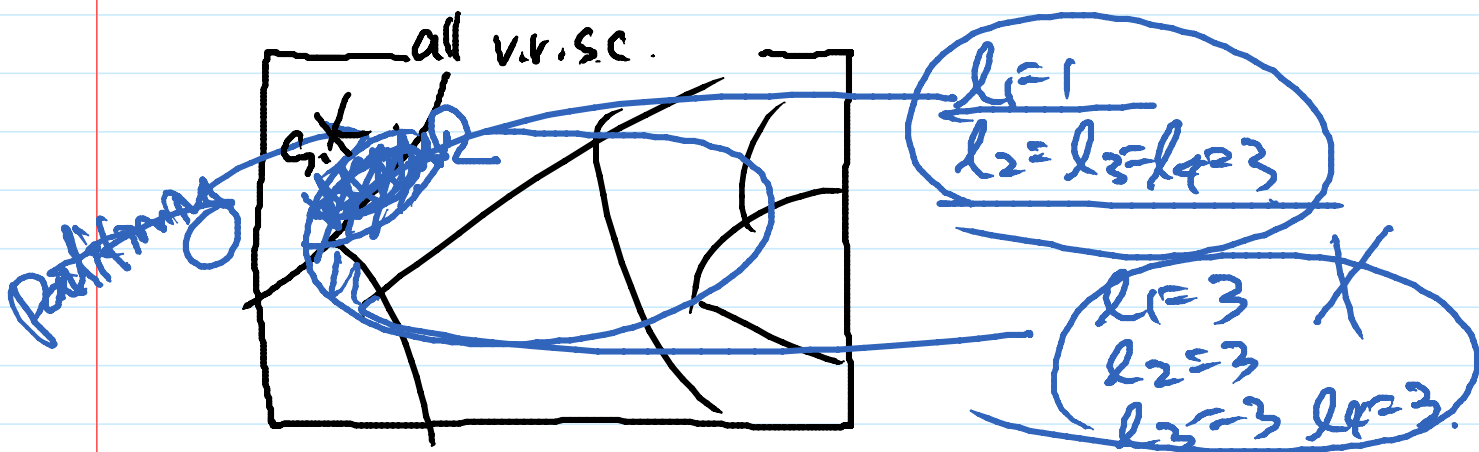


Upper bound

Tree Representation of a (v.r.) source code



Visualize! $\Rightarrow$ Too good to be true.



Definition $\begin{cases} \text{existence} \\ \text{uniqueness} \end{cases}$

Optimal solution $\begin{cases} \text{fully characterize} \\ \text{find an optimal solution} \end{cases}$

Summary

- Tree representation of a PF code
- Given a set of ^{any} UD codes w/
 $(l_1, l_2, \dots, l_n)$ s.t. $\sum_{i=1}^n D^{-l_i} \leq 1$,
we can always
find a PF code.